

What you will learn about:
Solving Equations Using Addition and Subtraction
Properties

Solution to Equation

Value that
make equation
true.

Determine whether a number is a solution to equation

Step 1 – Substitute the number in for the variable (5)

Step 2 – Simplify the expressions on both sides of the equation

Step 3 – Determine whether the resulting equation is true
(Left side is equal to the Right side)

If true, the number is a solution

If false the number is not a solution

Determine whether

$x = \frac{3}{2}$ is a solution of $4x - 2 = 2x + 1$

Solution

$$4\left(\frac{3}{2}\right) - 2 = 2\left(\frac{3}{2}\right) + 1$$

$$6 - 2 = 3 + 1$$

$$4 = 4$$

Is $y = \frac{7}{5}$ a solution of $5y + 3 = 10y - 4$

Solution

$$5\left(\frac{7}{5}\right) + 3 \stackrel{?}{=} 10\left(\frac{7}{5}\right) - 4$$

$$7 + 3$$

$$14 - 4$$

$$10 = 10$$

Subtraction Property of
Equality

$$a = b$$

$$a - c = b - c$$

Solve:

$$y + 37 = -13$$

$$-37 \quad -37$$

$$y = -50$$

$$x + 19 = 8$$

$$-19 \quad -19$$

$$x = -11$$

Addition Property of Equality

$$a = b$$

$$a + c = b + c$$

$$\frac{6}{8} + \frac{5}{8} = \frac{11}{8}$$

$$\begin{array}{r} 3 \text{ " } 10 \\ -4.20 \\ .63 \\ \hline -3.57 \end{array}$$

Solving Equations that require Simplification

Solve:

$$\begin{array}{r} a - 28 = -37 \\ +28 \quad +28 \\ \hline a = -9 \end{array}$$

$$\begin{array}{r} x - \frac{5}{8} = \frac{3}{4} + \frac{5}{8} \\ +\frac{5}{8} \\ \hline x = \frac{11}{8} \end{array}$$

$$\begin{array}{r} n - 0.63 = -4.2 \\ +0.63 \quad +0.63 \\ \hline n = -3.57 \end{array}$$

$$(9x - 5 - 8x - 6) = 7$$

$$x - 11 = 7$$

$$x = 18$$

$$\begin{array}{r} 5(x - 4) - 4x = -8 \\ 5x - 20 - 4x = -8 \\ x - 20 = -8 \\ +20 \quad +20 \\ \hline x = 12 \end{array}$$

$$\begin{array}{r} 3(2y - 1) - 5y = 2(y + 1) - 2(y + 3) \\ 6y - 3 - 5y = 2y + 2 - 2y - 6 \\ y - 3 = -4 \end{array}$$

$$y = -1$$

$$\begin{array}{r} n - 61 = -55 \\ +61 \quad +61 \\ \hline n = 6 \end{array}$$

$$\begin{array}{r} p - \frac{2}{3} = -\frac{5}{6} + \frac{2}{3} \\ +\frac{2}{3} \\ \hline p = -\frac{1}{6} \end{array}$$

$$\begin{array}{r} b - 0.47 = 1.23 \\ +.47 \quad .47 \\ \hline b = 1.70 \end{array}$$

$$(8y - 4 - 7y - 7) = -4$$

$$y - 11 = -4$$

$$y = 7$$

$$\begin{array}{r} 5(p - 3) - 4p = -5 \\ 5p - 15 - 4p = -5 \\ p - 15 = -5 \\ p = 10 \end{array}$$

$$-\frac{5}{6} + \frac{4}{6}$$

Translate to an equation and Solve

$$4(2h - 3) - 7h = 6(h - 2) - 6(h - 1)$$

$$8h - 12 - 7h = 6h - 12 - 6h + 6$$

$$h - 12 = -6$$

$$h = 6$$

Step 1- Locate the "equal" words
translate into = sign

Step 2- Translate words to the left
of equals into an Algebraic Expression

Step 3- Translate words to the Right of
equals into an Algebraic Expression

Translate and Solve:

Eleven more than x is equal to 54.

$$\begin{array}{rcl} x + 11 & = & 54 \\ -11 & -11 & \\ \hline \end{array} \quad x = 43$$

Translate and Solve:

Ten more than x is equal to 41.

$$x + 10 = 41$$

$$x = 31$$

Translate and Solve:

Twelve less than x is equal to 51.

$$x - 12 = 51$$

$$x = 63$$

Translate and Solve:

The difference of $12t$ and $11t$ is -14.

$$12t - 11t = -14$$

$$t = -14$$

The MacIntyre family recycled newspapers for two months. The two months of newspapers weighed a total of 57 pounds. The second month, the newspaper weighed 28 pounds. How much did the newspaper weigh in the first month?

$$\begin{array}{r} X + 28 = 57 \\ -28 \quad -28 \\ \hline \end{array}$$

$$X = 29 \text{ lbs}$$

Randell paid \$28,675 for his new car. This was \$875 less than the sticker price. What was the sticker price of the car?

$$\begin{array}{r} X - 875 = 28,675 \\ + 875 \quad \underline{875} \\ \hline X = \$29,550 \end{array}$$

The admission price for the movies during the day is \$7.75. This is \$3.25 less the price at night. How much does the movie cost at night?

$$\begin{array}{r} X - 3.25 = 7.75 \\ \quad \quad \quad \underline{3.25} \\ X = \$11.00 \end{array}$$

What you will learn about:
Solving Equations Using Division and Multiplication
Properties

Division Property of Equality

$$a = b$$

$$\frac{a}{c} = \frac{b}{c}$$

Multiplication Property of Equality

$$a = b$$

$$ac = bc$$

Solve:

$$\frac{5x}{5} = \frac{-27}{5}$$

$$x = -\frac{27}{5}$$

$$\frac{4z}{4} = \frac{-55}{4}$$

$$z = -\frac{55}{4}$$

$$(-7)\left(\frac{y}{-7}\right) = (-8)(-7)$$

$$y = 56$$

$$(-6)\left(\frac{b}{-6}\right) = (-24)(-6)$$

$$b = 144$$

$$4\left(\frac{3}{4}x\right) = (12)(4)$$

$$\frac{3x}{3} = \frac{48}{3}$$

$$x = 16$$

$$\left(\frac{4}{3}\right)\left(\frac{3}{4}x\right) = \left(\frac{4}{12}\right)\left(\frac{4}{8}\right)$$

$$x = 16$$

$$\left(\frac{6}{5}\right)\left(\frac{5}{6}y\right) = \left(\frac{15}{1}\right)\left(\frac{6}{5}\right)$$

$$y = 18$$

$$\frac{40}{15} \div -4$$

$$\frac{40}{15} \div -\frac{4}{1} = -\frac{10}{15}$$

$$\frac{40}{15} \cdot -\frac{1}{4} = -\frac{10}{15}$$

$$5\left(\frac{8}{15}\right) = \left(-\frac{4}{5}x\right)(5)$$

$$\frac{40}{15} = -4x$$

$$x = -\frac{10}{3}$$

$$3\left(\frac{5}{6}\right) = \left(-\frac{8}{3}r\right)(3)$$

$$\frac{15}{6} = -8r$$

$$14 - 23 = 12y - 4y - 5y$$

$$-9 = 3y$$

$$y = -3$$

$$-4(a - 3) - 7 = 25$$

$$-4a + 12 - 7 = 25$$

$$-4a + 5 = 25$$

$$-4a = 20$$

$$a = -5$$

$$\frac{24}{4} = 6$$

$$\frac{15}{6} \div -\frac{8}{1}$$

$$\frac{15}{6} \cdot -\frac{1}{8}$$

$$r = -\frac{15}{48}$$

$$r = -\frac{5}{16}$$

$$\begin{array}{r} 13 \\ 11 \overline{) 143} \\ \underline{11} \\ 33 \end{array}$$

$$-6(r - 2) - 12 = 30$$

$$-6r + 12 - 12 = 30$$

$$-6r = 30$$

$$r = -5$$

Translate and Solve:

The number 143 is the product of -11 and y.

$$143 = -11y$$

$$y = -13$$

n divided by 8 is -32.

$$8\left(\frac{n}{8}\right) = (-32)(8)$$

$$n = -256$$

The quotient of y and -4 is 68.

$$(-4)\left(\frac{y}{-4}\right) = (68)(-4)$$

$$y = -272$$

Three-fourths of p is 18.

$$\left(\frac{4}{3}\right)\left(\frac{3}{4}p\right) = (18)\left(\frac{4}{3}\right)$$

$$p = 24$$

The sum of three-eighths and x is one-half.

$$x + \frac{3}{8} = \frac{1}{2}$$

$$x = \frac{4}{8} - \frac{3}{8}$$

$$= \frac{1}{8}$$

$$\begin{array}{r} 1 \\ -32 \\ 8 \\ \hline -256 \end{array}$$

$$\begin{array}{r} 3 \\ 68 \\ 4 \\ \hline -272 \end{array}$$

$$\begin{array}{r} 1.79 \\ 6 \overline{) 10.74} \\ \underline{6} \\ 47 \\ \underline{42} \\ 54 \end{array}$$

$$\begin{array}{r} 5.83 \\ 4 \overline{) 34.98} \\ \underline{30} \\ 49 \\ \underline{48} \\ 18 \end{array}$$

$$\begin{array}{r} 12000 \\ 15 \overline{) 1,800,000} \\ \underline{15} \\ 30 \\ \underline{30} \end{array}$$

Denae bought 6 pounds of grapes for \$10.74. What was the cost of one pound of grapes?

$$\frac{10.74}{6} = p$$

$$6p = 10.74$$

$$p = \$1.79/1b$$

At JB's Bowling Alley, 6 people can play on one lane for \$34.98. What is the cost for each person?

$$6c = 34.98$$

$$c = \frac{34.98}{6}$$

$$c = \$5.83/\text{person}$$

Andreas bought a used car for \$12,000. Because the car was 4 years old, the price was $\frac{3}{4}$ of the original price, when the car was new. What was the original price of the car?

$$\left(\frac{4}{3}\right)\left(\frac{3}{4}\right)p = (12,000)\left(\frac{4}{3}\right)$$

$$p = \$16,000$$

The annual property tax on the Mehta's house is \$1,800, calculated as $\frac{15}{1,000}$ of the assessed value of the house.

What is the assessed value of the Mehta's house?

$$1000 \left(\frac{15}{1000} \cdot x \right) = (1800)(1000)$$

$$15x = 1,800,000$$

$$x = \$120,000$$

Stella planted 14 flats of flowers in $\frac{2}{3}$ of her garden. How many flats of flowers would she need to fill the the whole garden?

$$\frac{3}{2} \left(\frac{2}{3} \right) x = (14) \frac{3}{2}$$

$$x = 21 \text{ flats}$$